

# Learning Biological Regulatory Networks from Time Series with LFIT: Theory and Practice

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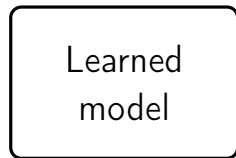
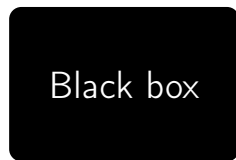
Workshop on network and model inference (CIRM)

Joint work with: Tony Ribeiro (Independent researcher, France),  
Omar Ikne (Univ. Lille, France),  
Morgan Magnin (Centrale Nantes, France),  
Katsumi Inoue (NII, Tokyo, Japan)

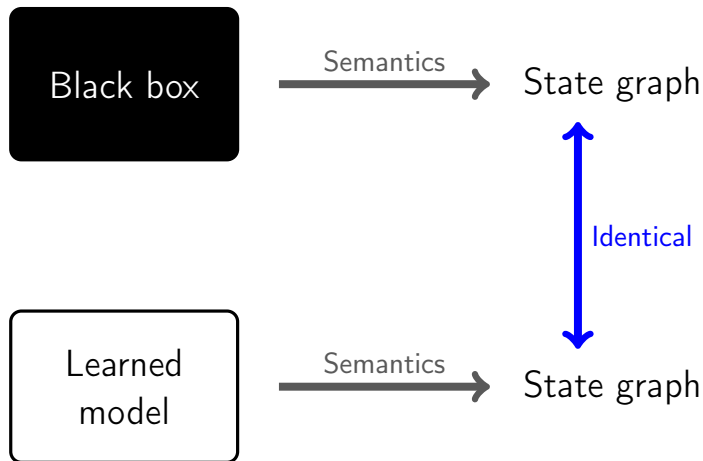
# Outline

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  - Semantics
  - Logic Rules
- 2 Learning From Interpretation Transition (LFIT)
  - Intuition
  - GULA
- 3 Two Heuristic on LFIT
  - Weighted Likelihood/Unlikelihood Rules
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- 4 Application: Dynamics of Marine Phytoplankton
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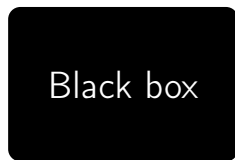
## Introduction



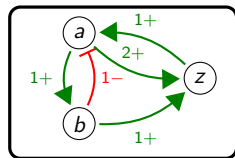
# Introduction



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State graph

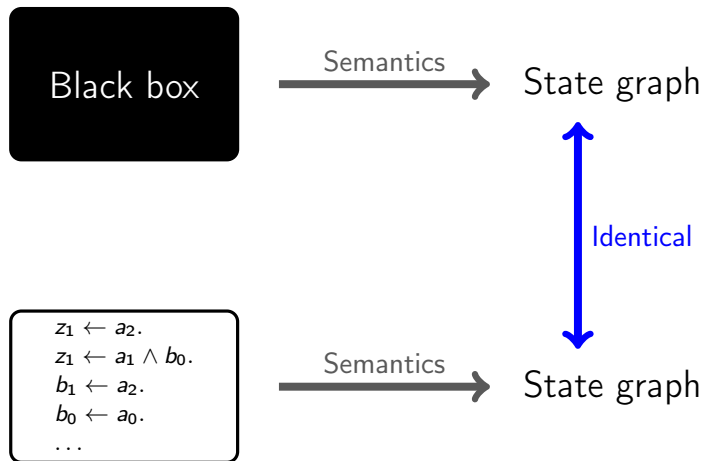


State graph



Identical

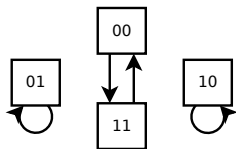
# Introduction



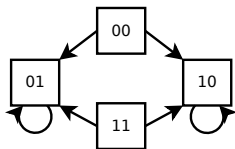
# General Definitions

## Dynamical Semantics

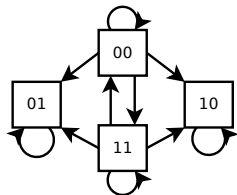
A Boolean network is a (syntactical) structure.  
It must be interpreted with a semantics to run.


 $f(a) := \text{not } b.$ 
 $f(b) := \text{not } a.$ 


Synchronous



Asynchronous



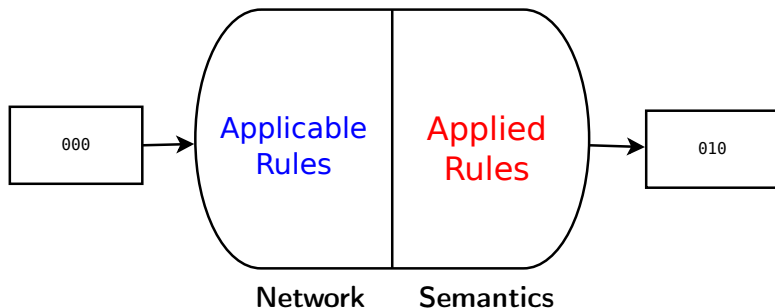
General

- **Synchronous:** all variables are updated
- **Asynchronous:** only one variable is updated
- **General:** any number of variables can be updated



## Definition of Semantics

In a given state, among the possible changes permitted by the network (structure), the semantics select which ones to apply and how to combine them.



## Logic Rules

LFIT learns a logic program, which is a set of logic rules.  
It is an alternative representation of biological networks.

$$a_1 \leftarrow a_0, b_0, c_2.$$

The network states that if  $a$  and  $b$  are at level 0 and  $c$  is at level 2, then  $a$  can change its value to 1.

$$a_1 \leftarrow c_2.$$

Whenever  $c$  is at level 2,  $a$  can change its value to 1.

$$a_1 \leftarrow .$$

$a$  can change its value to 1 anytime.

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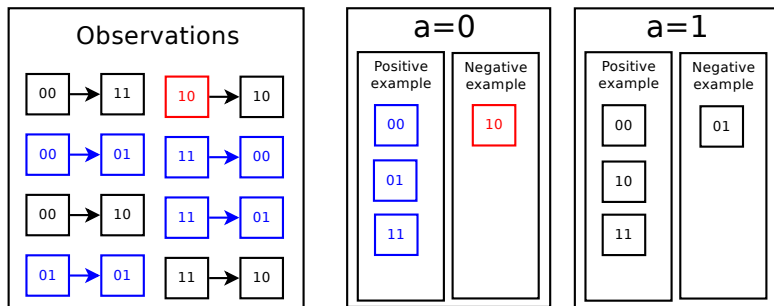
$a$  **can** change its value to 1 anytime.

When **will**  $a$  take value 1? This depends on the semantics

# Learning From Interpretation Transition (LFIT)

## Learning Algorithm Intuition: Classification Problem

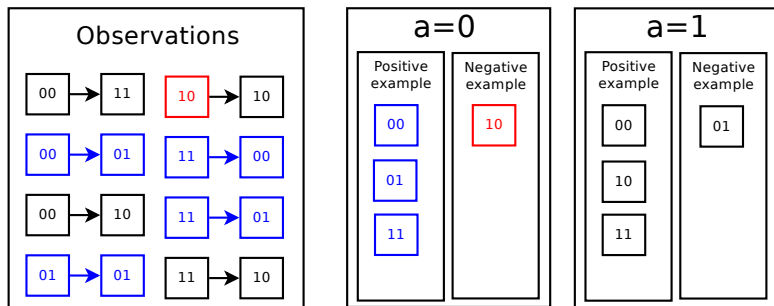
Learn applicable rules: conditions so that a variable **can** take a certain value in next state.



Equivalent to a **classification problem**: What is a typical state where  $a$  can take value 0 in the next state? Here: when  $a_0$  or  $b_1$  is present.

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Equivalent to a **classification problem**: What is a typical state where  $a$  can take value 0 in the next state? Here: when  $a_0$  or  $b_1$  is present.

$$a_0 \leftarrow a_0. \quad a_0 \leftarrow b_1.$$

# Presentation of GULA

**GULA** = General Usage LFIT Algorithm

**Input:** a set of transitions ( $s_1 \rightarrow s_2$ )

**Output:** a logic program that respects:

- **Consistency:** the program allows no negative examples
- **Realization:** the program covers all positive examples
- **Completeness:** the program covers all the state space
- **Minimality** of the rules (most general conditions)

**Method:** start from most general rules and **specialize** iteratively.

## Minimal refinements

Suppose:  $\text{dom}(a) = \text{dom}(b) = \{0, 1\}$  and  $\text{dom}(c) = \{0, 1, 2\}$   
and the current program contains the following rules regarding  $a_1$ :

$$a_1 \leftarrow c_2.$$

$$a_1 \leftarrow b_1.$$

From state  $\langle a_1, b_0, c_2 \rangle$ ,  $a_1$  is never observed in the next states.

**Minimal refinement** to make the rules inapplicable in this state:



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$$a_1 \leftarrow c_2, c_0.$$

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$$a_1 \leftarrow b_1.$$

(No change)

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(More general)

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## Results

Tony Ribeiro, Maxime Folschette, Morgan Magnin and Katsumi Inoue.  
**Learning any memory-less discrete semantics for dynamical systems represented by logic programs.** *Machine Learning* 111, Springer.  
November 2021. <https://doi.org/10.1007/s10994-021-06105-4>

- **Allows to learn the network** (structure of the model)
- **Independent of the semantics**  
(characterization of applicable memoryless semantics)

Nice in theory, but in practice?

- **Exponential complexity** → How to handle big datasets?  
(many transitions, many variables)
- **Exact learning** → How to handle noise?

# Two Heuristic on LFIT

# Weighted Likelihood/Unlikelihood Rules

- Use the algorithm twice to learn two logic programs:
  - ▶ likelihood rules: what is possible
  - ▶ unlikelihood rules: what is impossible
- Weight each rule by the number of observations it matches

Statistical overlay  $\Rightarrow$  usable on **noisy datasets**

## Likelihood rules

$$(3, a_0 \leftarrow b_1)$$

$$(15, a_1 \leftarrow b_0)$$

$$\vdots$$

## Unlikelihood rules

$$(30, a_0 \leftarrow c_1)$$

$$(5, a_1 \leftarrow c_0)$$

$$\vdots$$

## Using Weighted Likelihood/Unlikelihood Rules

### Explainable predictions:

- Compare weights of applicable likelihood/unlikelihood rules
- Ratio of highest weights  $\Rightarrow$  **probability**  $P$
- Rules with highest weights  $\Rightarrow$  **explanation**  $E$

predict : (*atom*, *state*)  $\mapsto$  ( $P$ ,  $E$ )

#### Likelihood rules

(3,  $a_0 \leftarrow b_1$ )

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predict :  $(atom, state) \mapsto (P, E)$

#### Likeliness rules

$(3, a_0 \leftarrow b_1)$

$(15, a_1 \leftarrow b_0)$

#### Unlikeliness rules

$(30, a_0 \leftarrow c_1)$

$(5, a_1 \leftarrow c_0)$

predict( $a_1, \langle a_1, b_1, c_0 \rangle$ ) =  $(0.75, ((15, a_1 \leftarrow b_0), (5, a_1 \leftarrow c_0))) \Rightarrow$  Likely

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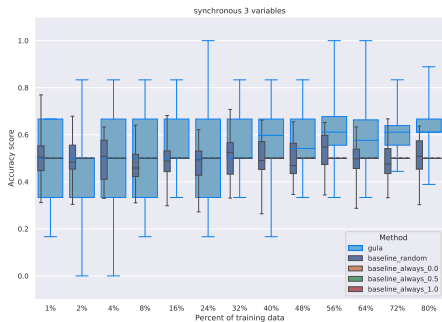
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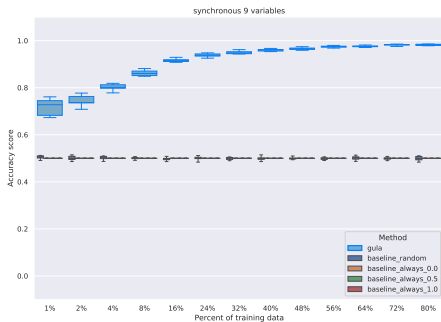
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predict( $a_0$ ,  $\langle a_1, b_1, c_0 \rangle$ ) = (0.09, ((3,  $a_0 \leftarrow b_1$ ), (30,  $a_0 \leftarrow c_1$ )))  $\Rightarrow$  Unlikely

# Prediction power



3 variables



9 variables

Training data =  $X\%$  of transitions

Tested against unseen states (not in the training data)

## PRIDE: Polynomial Alternative to GULA

**GULA: Exponential complexity** in the number of variables

**PRIDE:** Greedy version of **GULA** that only keeps the first compatible minimal refinement  $\Rightarrow$  subset of rules

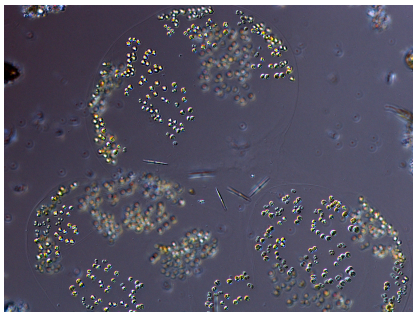
- **Consistency:** the program allows no negative examples
- **Realization:** the program covers all positive examples
- ~~Completeness: the program covers all the state space~~
- **Minimality** of the rules (most general conditions)

...And the results depends on the ordering of variables

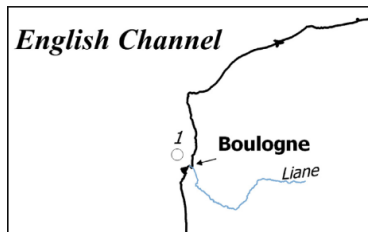
**Polynomial complexity**  $\Rightarrow$  usable on **large datasets**

# Application: Dynamics of Marine Phytoplankton

# Phytoplankton Blooms



## SRN Dataset



<https://www.seaonoe.org/data/00397/50832/>

Sampling location	Sampling date	Taxon	Value	Sampling depth
001-P-015	1992-05-18	CHLOROA	6.0	Surface (0-1m)
006-P-001	2019-12-02	Chaetoceros	1000.0	Surface (0-1m)
002-P-007	1994-05-25	Pleurosigma	100.0	Surface (0-1m)
002-P-030	2005-10-19	SALI	34.83	Surface (0-1m)
006-P-007	2015-09-28	Guinardia delicatula	11400.0	Surface (0-1m)

Environmental variables (7)

Phytoplankton species (12)

# Applying LFIT

## Expectations

- Find known **abiotic** influences (of environment on phytoplankton)
- Find new **biotic** influences (of phytoplankton species on others)

## Input

- Pre-processing: data cleaning + discretization
- 253 training transitions
- 53 testing transitions

## Output

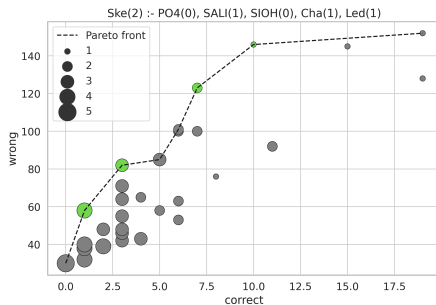
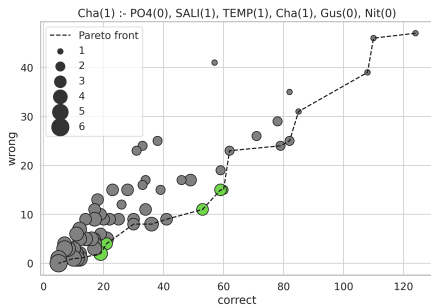
- Run time = 2.35s (**PRIDE**)
- 1683 likeliness rules
- 1981 unlikeliness rules
- Model accuracy: **0.670**



# Model Improvement

## Pareto frontier

- For likeliness rules : **maximize** correct and **minimize** wrong weights
- For unlikeliness rules : **maximize** wrong and **minimize** correct weights



Accuracy improvement: 0.670 → 0.716

Likelihood rules: 1683 → 1609

Unlikelihood rules: 1981 → 1405

## Global Influences

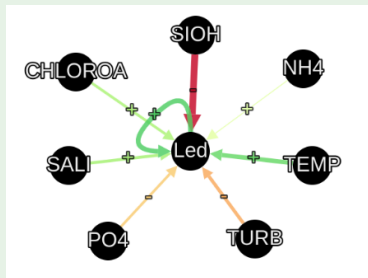
**Process:** Search and count patterns in rules that characterize an activation/inhibition

**Hypotheses:** Monotonous influences & same threshold for all variables

**Result:** Score  $[-1; +1]$  between each pair of variables (no threshold)

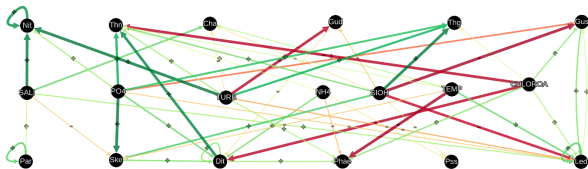
**Influences on phytoplankton specie Led:**

Variable	Positive	Negative	Global
P04	+0	-58	-0.36
SALI	+71	-4	+0.42
CHLOROA	+84	-22	+0.39
SIOH	+3	-161	-0.98
NH4	+25	-5	+0.12
TEMP	+106	-5	+0.63
TURB	+10	-87	-0.48

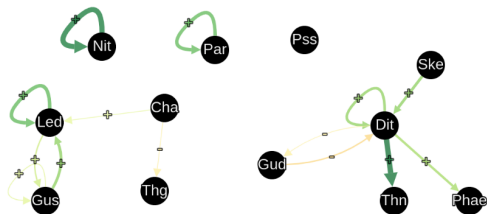


$$\text{global\_influence}(P04 \rightarrow \text{Led}) = \frac{+0 + (-58)}{161} = -0.36$$

## Results



Global influence graph (biotic and abiotic interactions)



Biotic interactions (between phytoplankton only)

Very few biotic interactions...

Future work: integrate knowledge + validate results

# Conclusion

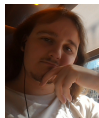
# Conclusion

- **Learn** the network with LFIT (theory)
- **Heuristics** to tackle real data (practice)
- **Application** to phytoplankton

## Outlooks:

- Quantify how many rules are “missed” by PRIDE
- Integrate biological knowledge to improve learning
- Improve the Biological network inference
- ...

# Thanks



**Tony  
RIBEIRO**



**Omar  
IKNE**



**Morgan  
MAGNIN**



**Katsumi  
INOUE**



**Cédric  
LHOSSAINE**



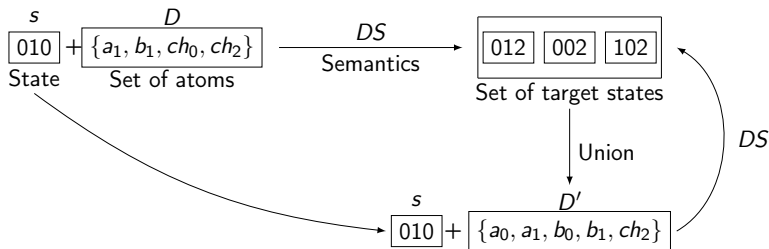
**Sébastien  
LEFEBVRE**

## Bibliography

- **About GULA:** Tony Ribeiro, Maxime Folschette, Morgan Magnin and Katsumi Inoue. **Learning any memory-less discrete semantics for dynamical systems represented by logic programs.** *Machine Learning* 111, Springer. November 2021.  
<https://doi.org/10.1007/s10994-021-06105-4>
- **pyLFIT Python library:** <https://github.com/Tony-sama/pylfit>
- **About PRIDE:** Tony Ribeiro, Maxime Folschette, Morgan Magnin and Katsumi Inoue. **Polynomial Algorithm For Learning From Interpretation Transition.** Poster at the *1st International Joint Conference on Learning & Reasoning*. October 2021, Online.  
<https://hal.science/hal-03347026v1>
- **About the application:** Omar Iken, Maxime Folschette and Tony Ribeiro. **Automatic Modeling of Dynamical Interactions Within Marine Ecosystems.** Poster in the *1st International Joint Conference on Learning & Reasoning*. October 2021, Online.  
<https://hal.science/hal-03347033v1>

## Pseudo-idempotent semantics

**GULA** can model observations from any **pseudo-idempotent** semantics.



$$\longrightarrow DS(s, D) = DS(s, \bigcup_{s' \in DS(s, D)} s')$$

where  $DS$  is the dynamical semantics, and  $D$  is set of heads of rules of a multi-valued logic program that match the state  $s$ .