

# **Towards the use of Process Hitting to tackle biological observations inconsistent with background knowledge**

**Joint work: Yoshitaka Yamamoto (1), Morgan Magnin  
(2,3,4), Maxime Folschette (2), Katsumi Inoue (3)**

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**(2) Ecole Centrale de Nantes, IRCCyN, Nantes, France**

**(3) National Institute of Informatics, Tôkyô, Japan**

**(4) JSPS Fellow**

# Motivations

- Given an existing network (**background knowledge**) and a (**new**) **observation** that is **inconsistent** with this network, how can we automatically design **the minimal set of missing actions that can mimic the observation?**
- Process Hitting is an efficient framework to cope with **large** networks (~ 100 components)

# Motivations

- Our proposition: design a method taking advantage of the Process Hitting methods to address the **completion of networks with inconsistent observations**
- Restrictions w.r.t. current work:
  - Consider **only addition of actions**, not removal of actions
  - Modeling of the evolution of a gene expression in case of ko w.r.t. wild type, under **steady state assumption**

# Overview

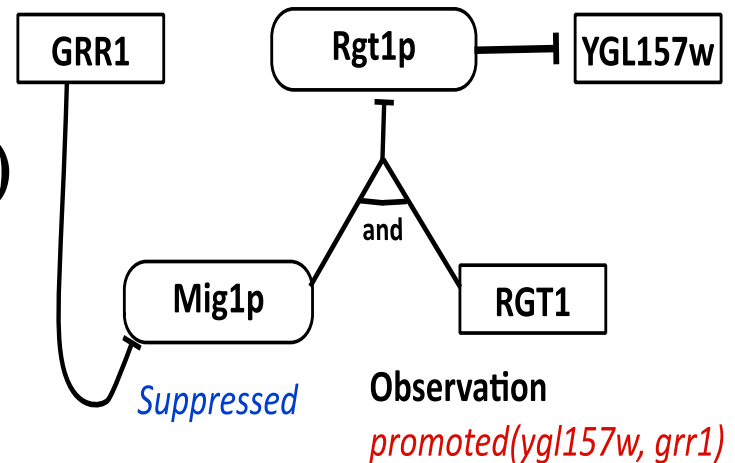
- Motivating example
- Reminder about the Process Hitting framework
- 4-level based logics and associated truth tables
- Translating 4-level based models into Process Hitting
- Further discussions

# Motivating example

□ Background theory *B*: Boolean network consisting of the three Boolean functions

- $Mig1p = \text{not } GRR1$
- $Rgt1p = \text{not } (Mig1p \ \& \ RGT1)$
- $YGL157w = \text{not } Rgt1p$

□ Observation *O*:



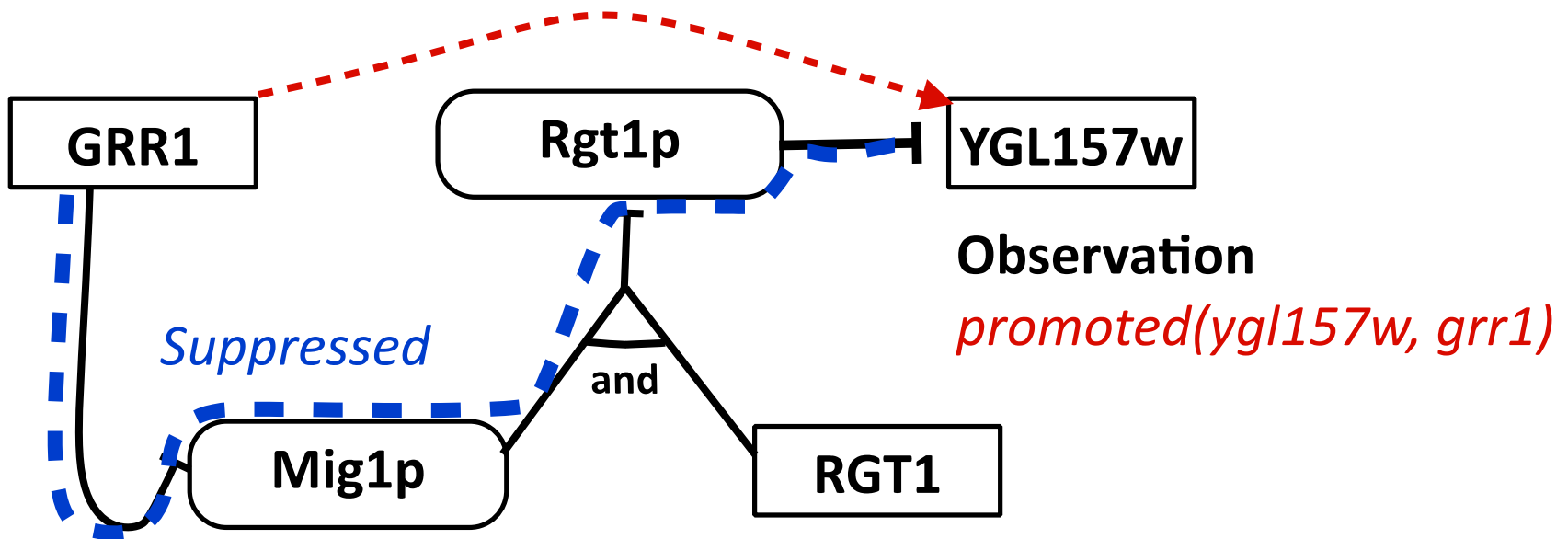
*When GRR1 is ko, then the gene expression of YGL157w decreases, i.e.:*

When the gene expression of GRR1 decreases, the gene expression of YGL157w also decreases.

( we write it by ***promoted(ygl157w, grr1)*** )

# Inconsistency between B and O

- Given the following initial state, we meet the fact that the gene expression of YGL157w decreases  
< **GRR1 = -1**, Mig1p = 0, Rgt1p = 0, RGT1 = 0, YGL157w = 0 >  
⇒ This is *inconsistent* with the observation...

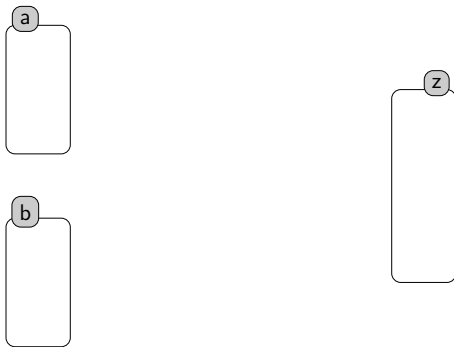


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- 4-level based logics and associated truth tables
- Translating 4-level based models into Process Hitting
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# The Process Hitting modelling

[Paulevé et al., *Transactions on Computational Systems Biology*, 2011]

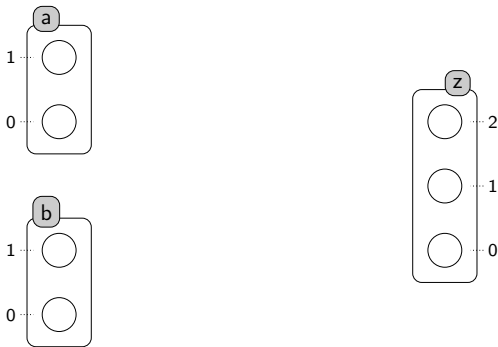


**Sorts:** components *a, b, z*



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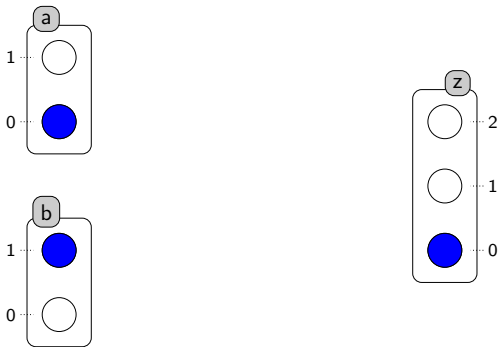


**Sorts:** components  $a, b, z$

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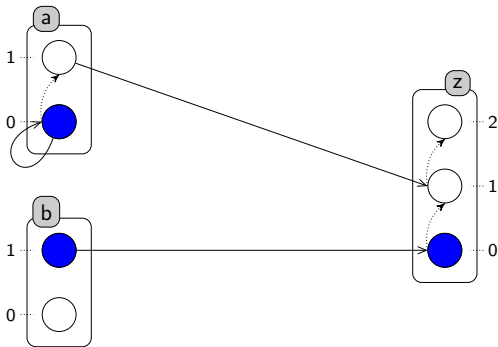
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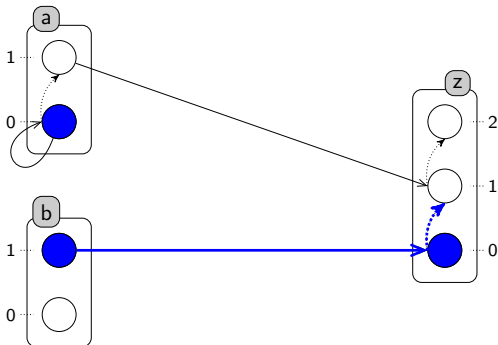
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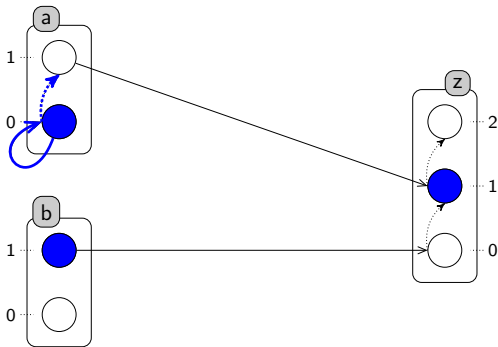
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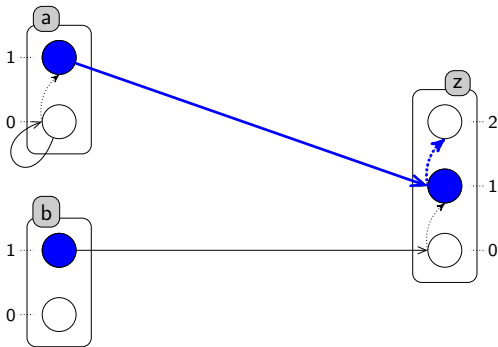
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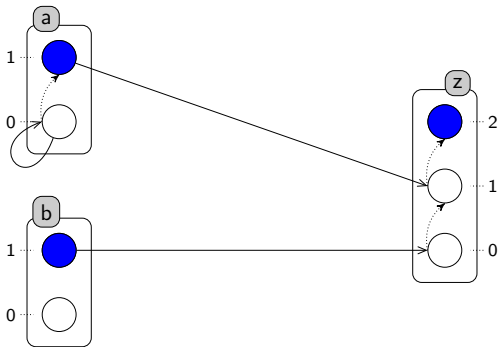
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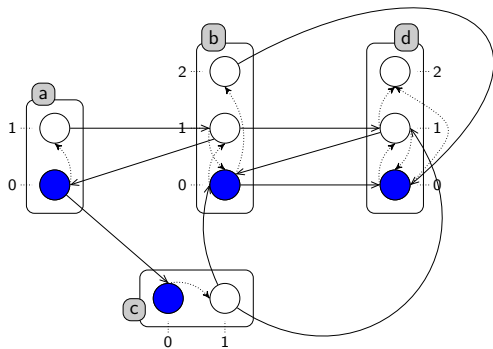
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[Paulevé et al., *Mathematical Structures in Computer Science*, 2012]



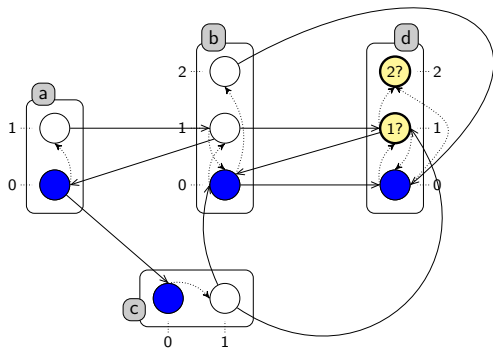
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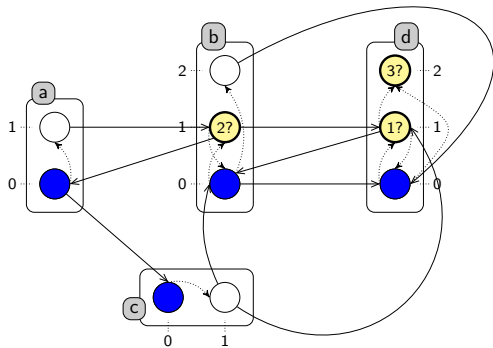
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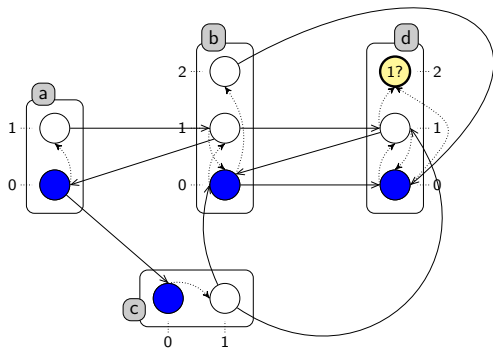
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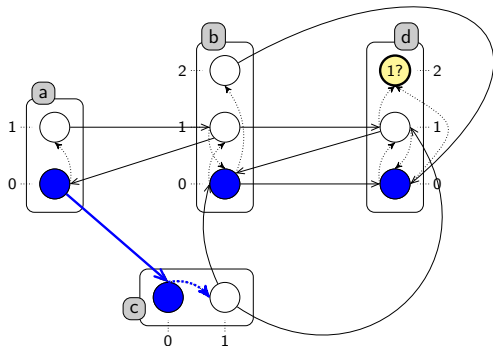
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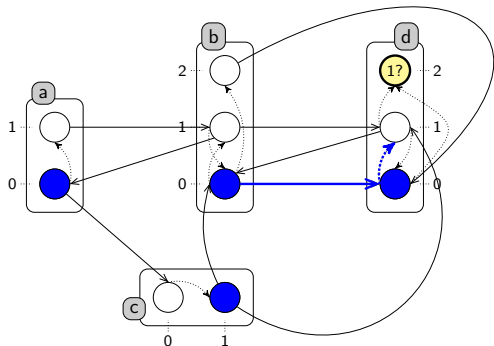
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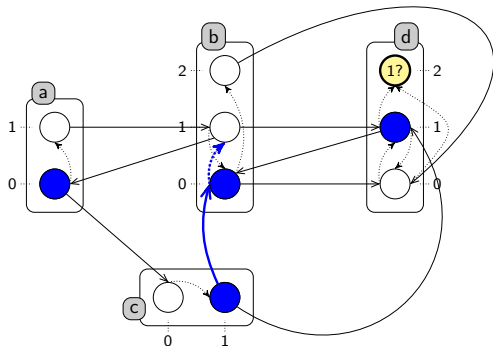
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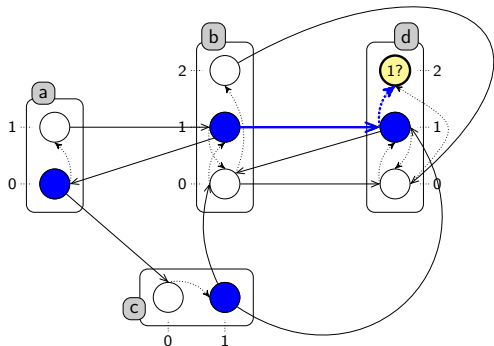
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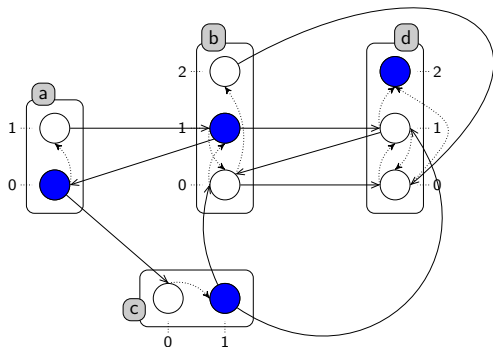
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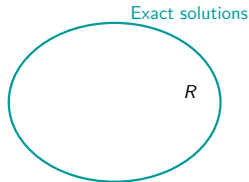


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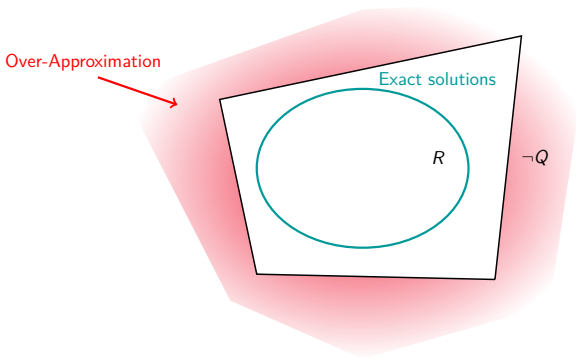
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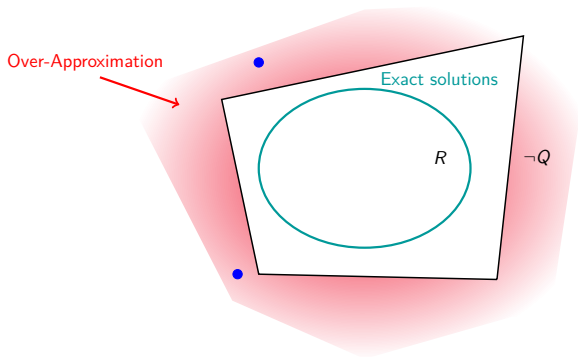


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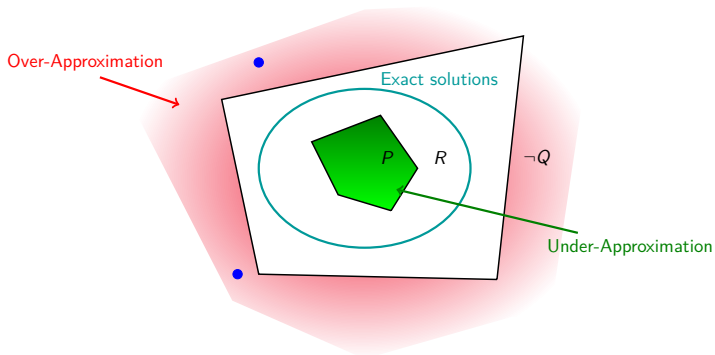


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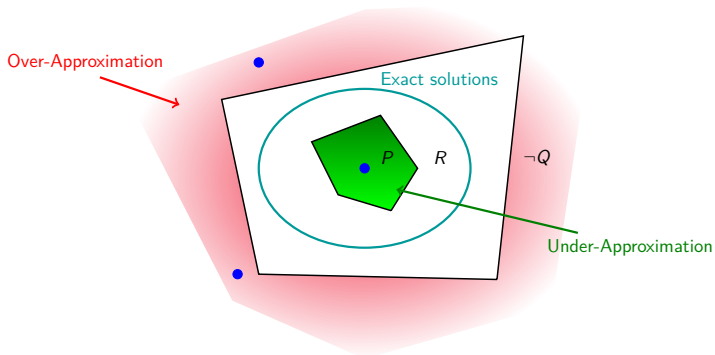
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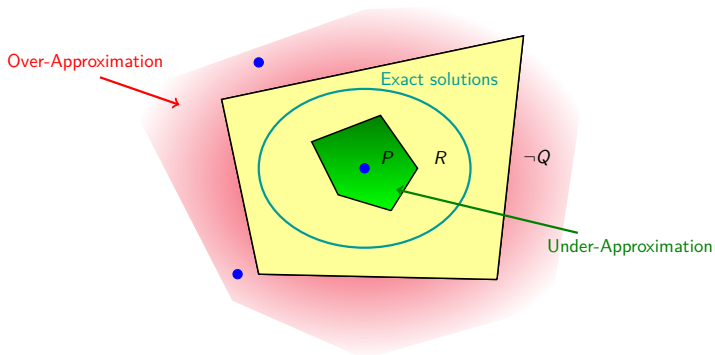


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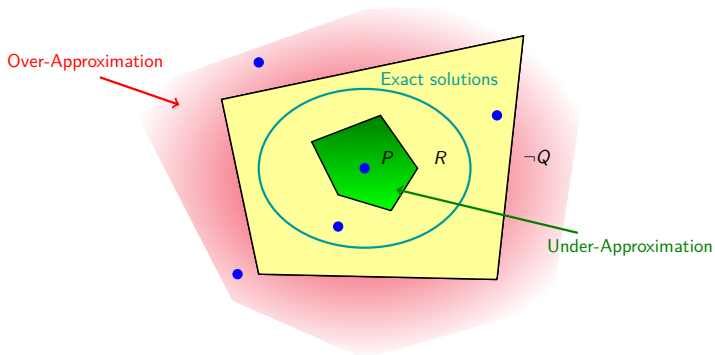
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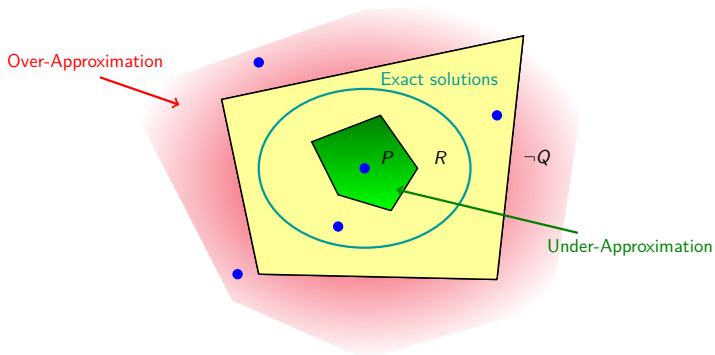
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Computing  $P$  or  $Q$  is much simpler (roughly **polynomial**)

- Efficient for big models → **Hundredths of seconds**



# Enrichment of the Process Hitting

[Folschette *et al.*, *CS2Bio'13*, 2013]

Several additions to improve the expressiveness of the Process Hitting:

- Priorities
  - Groups of actions with similar temporal/probabilistic parameters
- Neutralizing edges
  - Atomistic delay relations between actions
- Synchronous actions
  - Multiple reactants and products → Biochemical reactions

All these formalisms can be translated to a canonical form

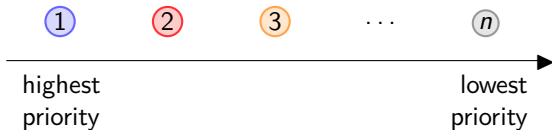
A new static analysis has been developed to check reachability properties

→ Efficient dynamic analysis on large models

# Priorities

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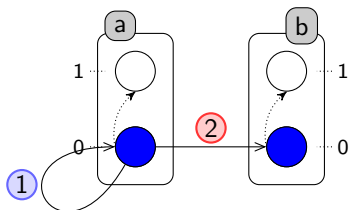
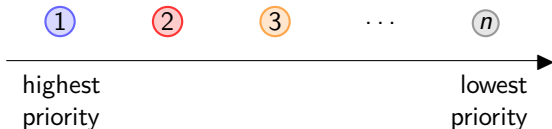
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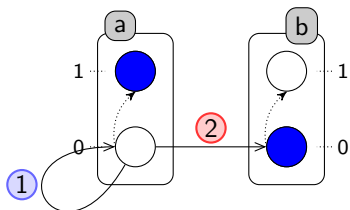
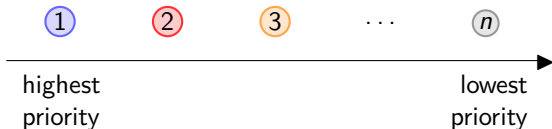


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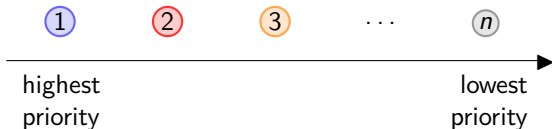


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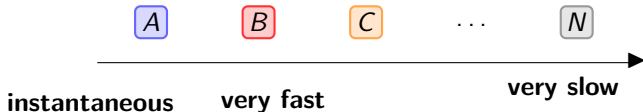
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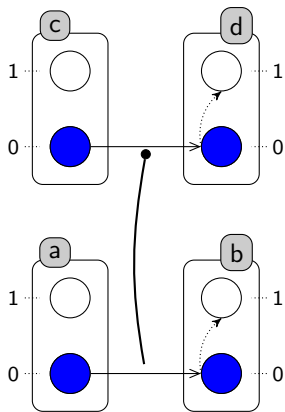
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- Allows to model classes of actions with similar temporal/stochastic parameters



## Neutralizing edges



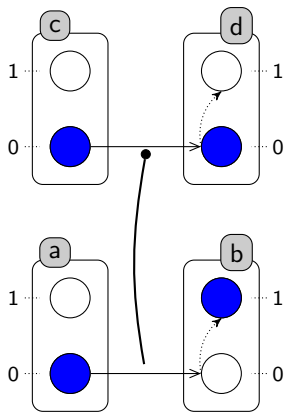
- Allows to integrate temporal data about relative reaction delays
- Atomistic preemptions

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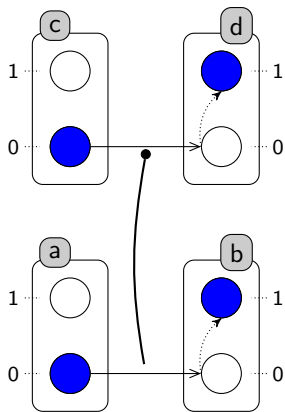
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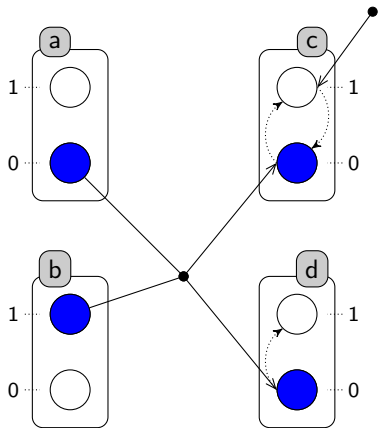
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# Synchronous actions



- Synchronization between actions:
  - Presence of catalysts
  - Consumption of reactants
  - Creation of products

- Convenient for biochemical equations:  
 $X \xrightarrow{Y} Z$   
in the following form:

$$\{X_1, Y_1, Z_0\} \rightsquigarrow \{X_0, Z_1\}$$

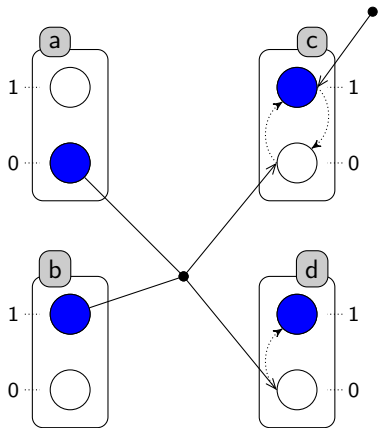
$$h_1 = \{c_1\} \rightsquigarrow \{c_0\}$$

$$h_2 = \{a_0, b_1, c_0, d_0\} \rightsquigarrow \{c_1, d_1\}$$

All processes of  $A$   
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After playing  $A \rightsquigarrow B$ ,  
all processes of  $B$  are active

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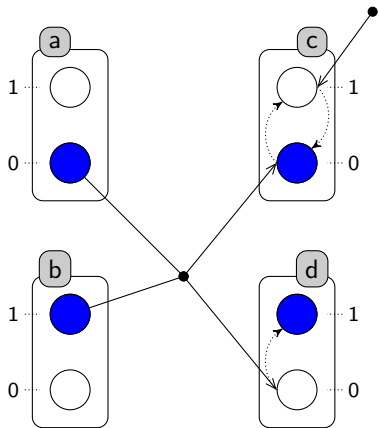
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- Convenient for biochemical equations:  
 $X \xrightarrow{Y} Z$   
in the following form:  
 $\{X_1, Y_1, Z_0\} \rightsquigarrow \{X_0, Z_1\}$

$$h_1 = \{c_1\} \rightsquigarrow \{c_0\}$$
$$h_2 = \{a_0, b_1, c_0, d_0\} \rightsquigarrow \{c_1, d_1\}$$

All processes of  $A$   
must be present to play  $A \rightsquigarrow B$

After playing  $A \rightsquigarrow B$ ,  
all processes of  $B$  are active

# Overview

- Motivating example
- Reminder about the Process Hitting framework
- **4-level based logics and associated truth tables**
- Translating 4-level based models into Process Hitting
- Further discussions

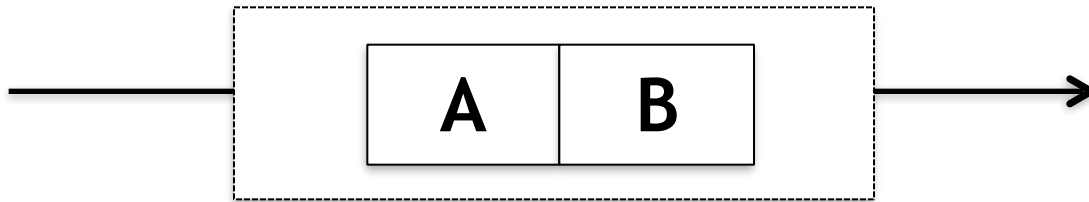
# Modeling ideas

- 4 cases to consider:
  - The concentration of a component  $c$  in  $ko$  of a given gene  $g$  is **higher** than its concentration in Wild Type (which will be denoted  $\uparrow$ )
  - The concentration of a component  $c$  in case of  $ko$  of a given gene  $g$  is **lower** than its concentration in Wild Type (which then will be denoted  $\downarrow$ )
  - The concentration of a component  $c$  in case of  $ko$  of a given gene  $g$  is **stable** compared to Wild Type (which then will be denoted  $-$ )
  - When the evolution of the concentration of a component  $c$  between  $ko$  and wild type is **unknown**: add a fourth level « unknown" in the logical framework, but not necessary in the Process Hitting final representation.

# Our stoichiometric modeling

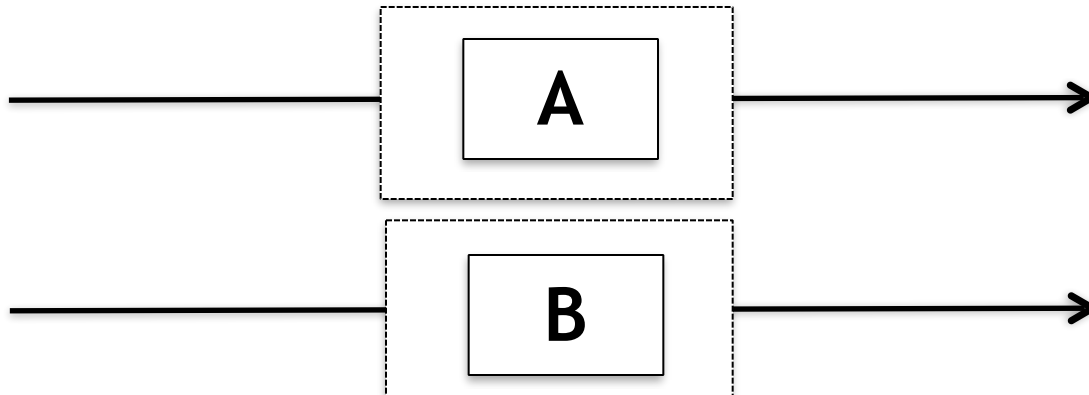
- **A and B**: denoting the effect by *the complex* of A and B

⇒ Strength: depending on the amount of the complex



- **A or B**: denoting the (individual) effects by A and B

⇒ Strength: depending on the amount of both A and B



# Truth table in 4 valued logic (1/2)

↑: increase. ↓: decrease. -: unchanged.

A	B	A and B	A or B
↑	↑	↑	↑
↑	↓	↓	<i>unknown</i>
↑	-	-	↑
↑	<i>unknown</i>	<i>unknown</i>	<i>unknown</i>
↓	↓	↓	↓
↓	-	↓	↓
↓	<i>unknown</i>	↓	<i>unknown</i>
-	-	-	-
-	<i>unknown</i>	<i>unknown</i>	<i>unknown</i>
<i>unknown</i>	<i>unknown</i>	<i>unknown</i>	<i>unknown</i>

# Truth table in 4 values logic (2/2)

↑: increase. ↓: decrease. -: unchanged.

A	$\neg A$
↑	↓
↓	↑
-	-
<i>unknown</i>	<i>unknown</i>



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# Principle of the translation of « 4 valued logics » into PH

- When A has more than one regulator, use a **cooperative sort** to update A according to the state of regulators → need to use **priorities** in PH
- « unknown » is modeled by modeling every potential underlying behavior

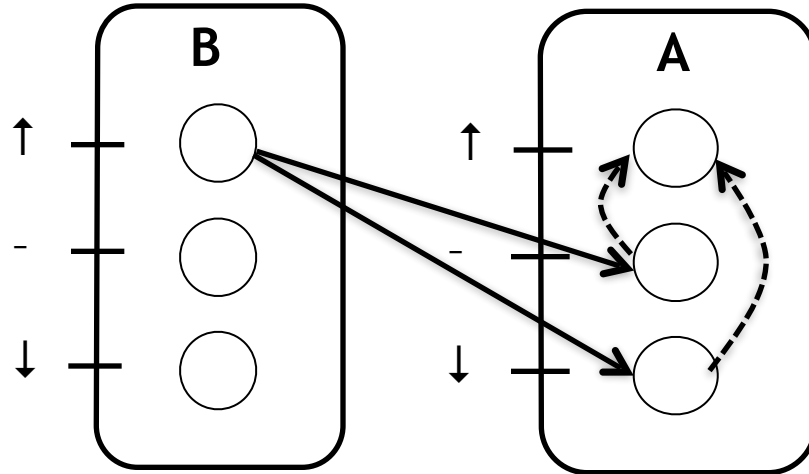
# Translating 4 valued logics into Process Hitting: $A=B$

1.  $A = B$

2.  $A = \text{not } B$

3.  $A = B \text{ and } C$

4.  $A = B \text{ or } C$



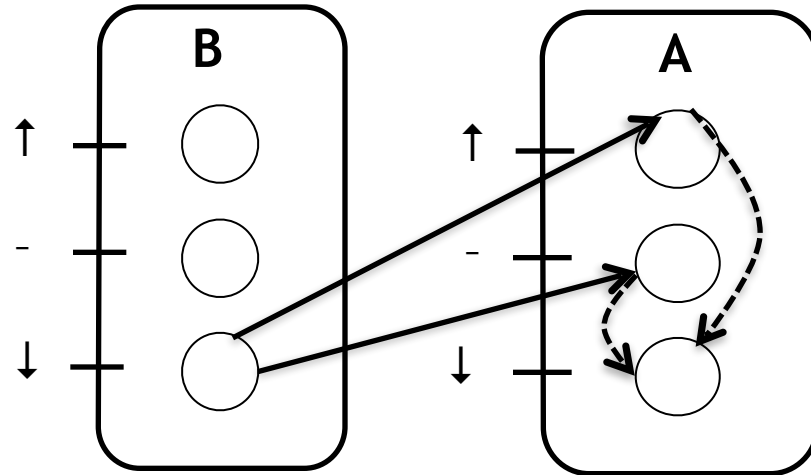
# Translating 4 valued logics into Process Hitting

1.  $A = B$

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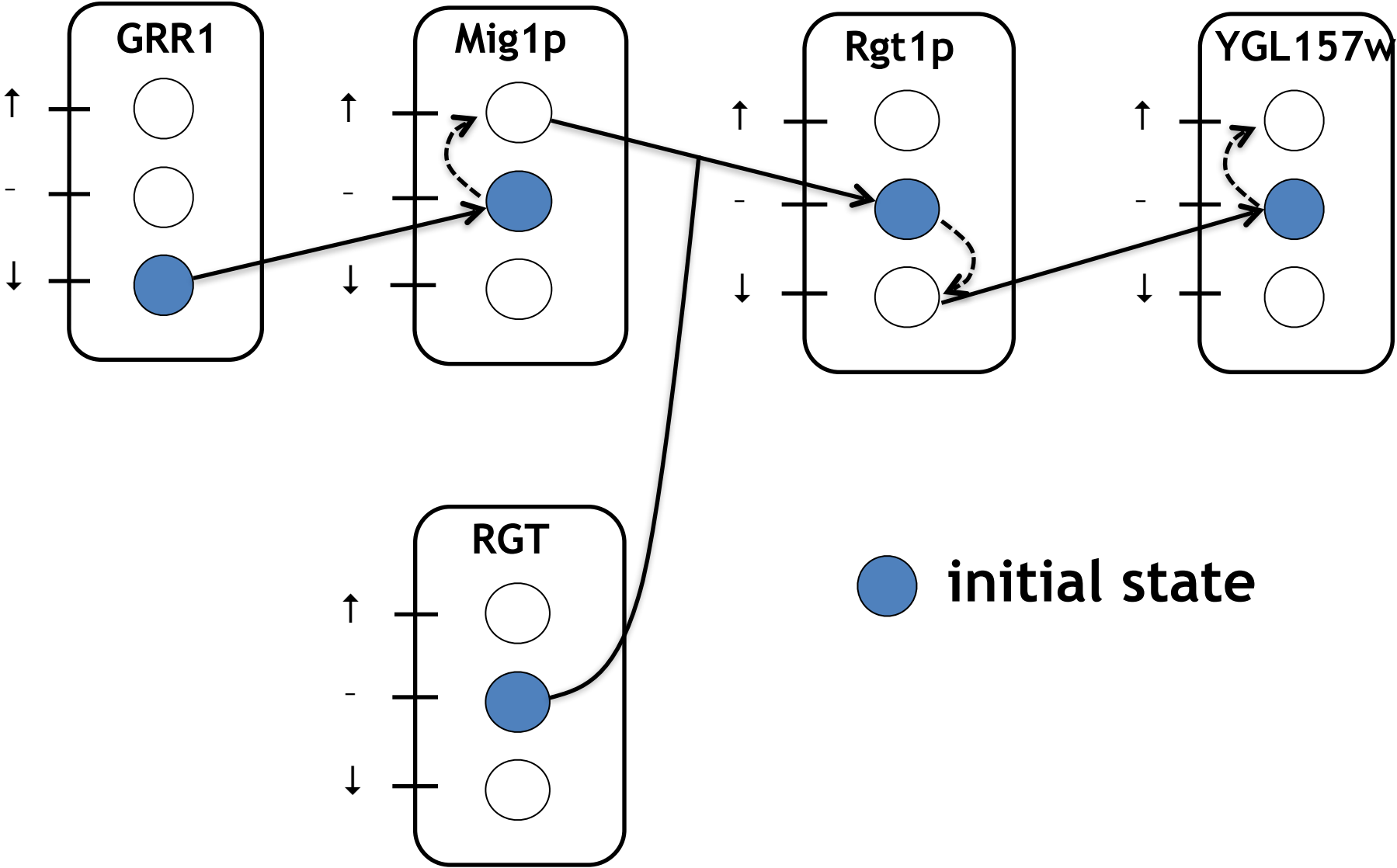
3.  $A = B \text{ and } C$

4.  $A = B \text{ or } C$

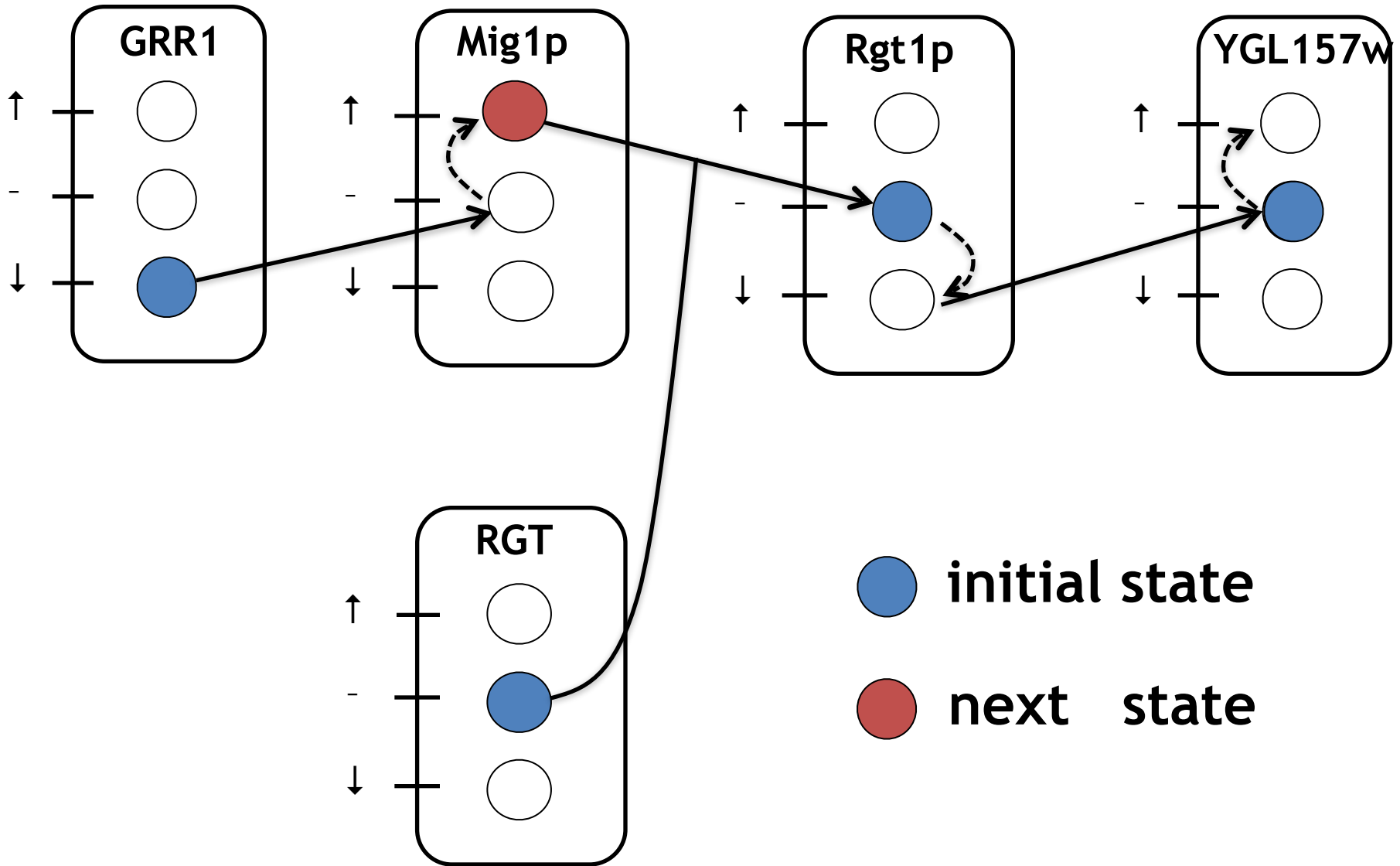


- Maybe add a slide with the translation of  $A = B$  and  $C$ , but the resulting PH is quite complex ?

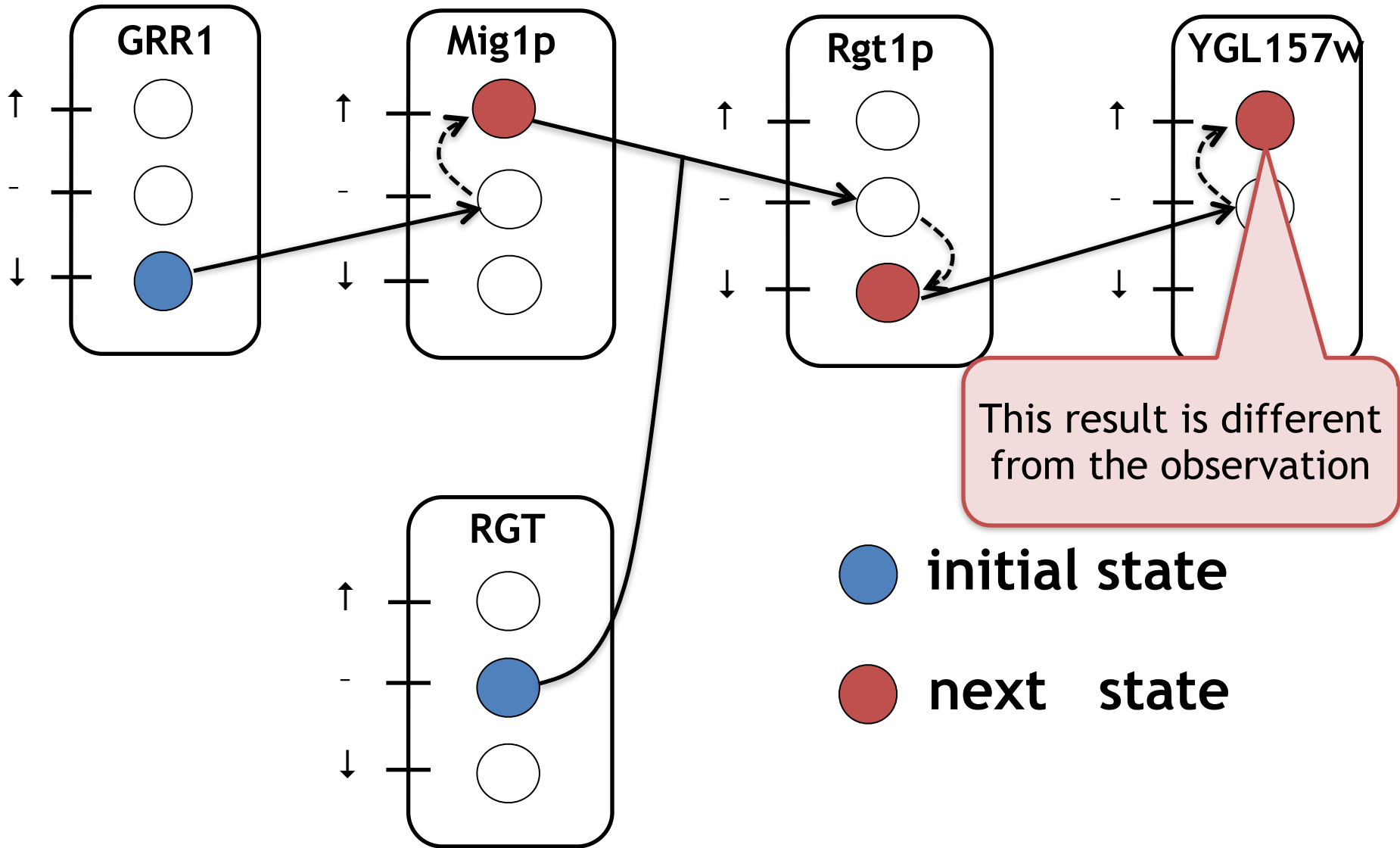
# Back to the example



# Back to the example: one execution

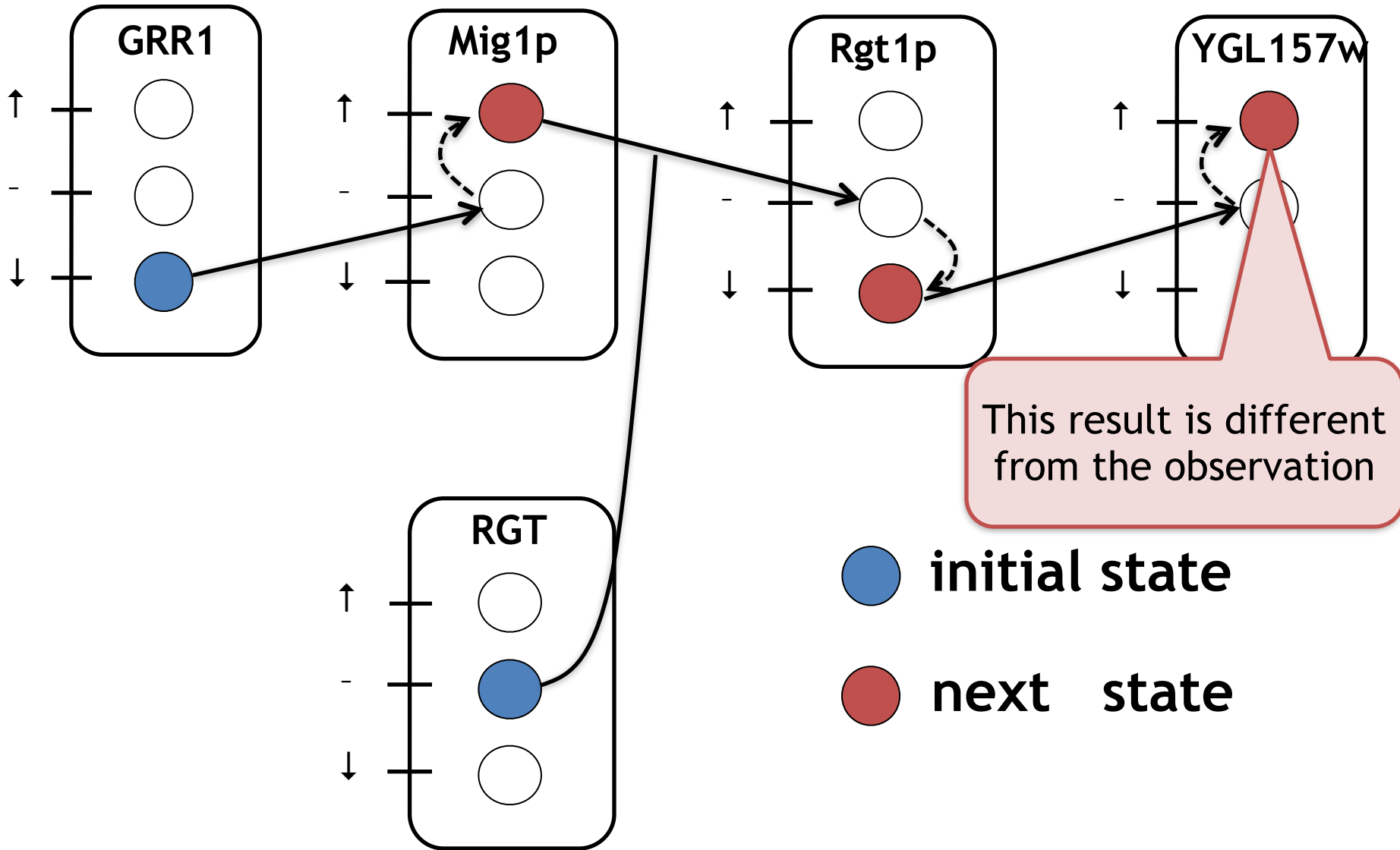


# Back to the example: one execution





# And with synchronous semantics?



# Our question

In case that the dynamics of the model does not encompass the observation into any playable scenario of actions... how to **detect missing actions as few as possible** that can lead the goal state?

# Related discussions

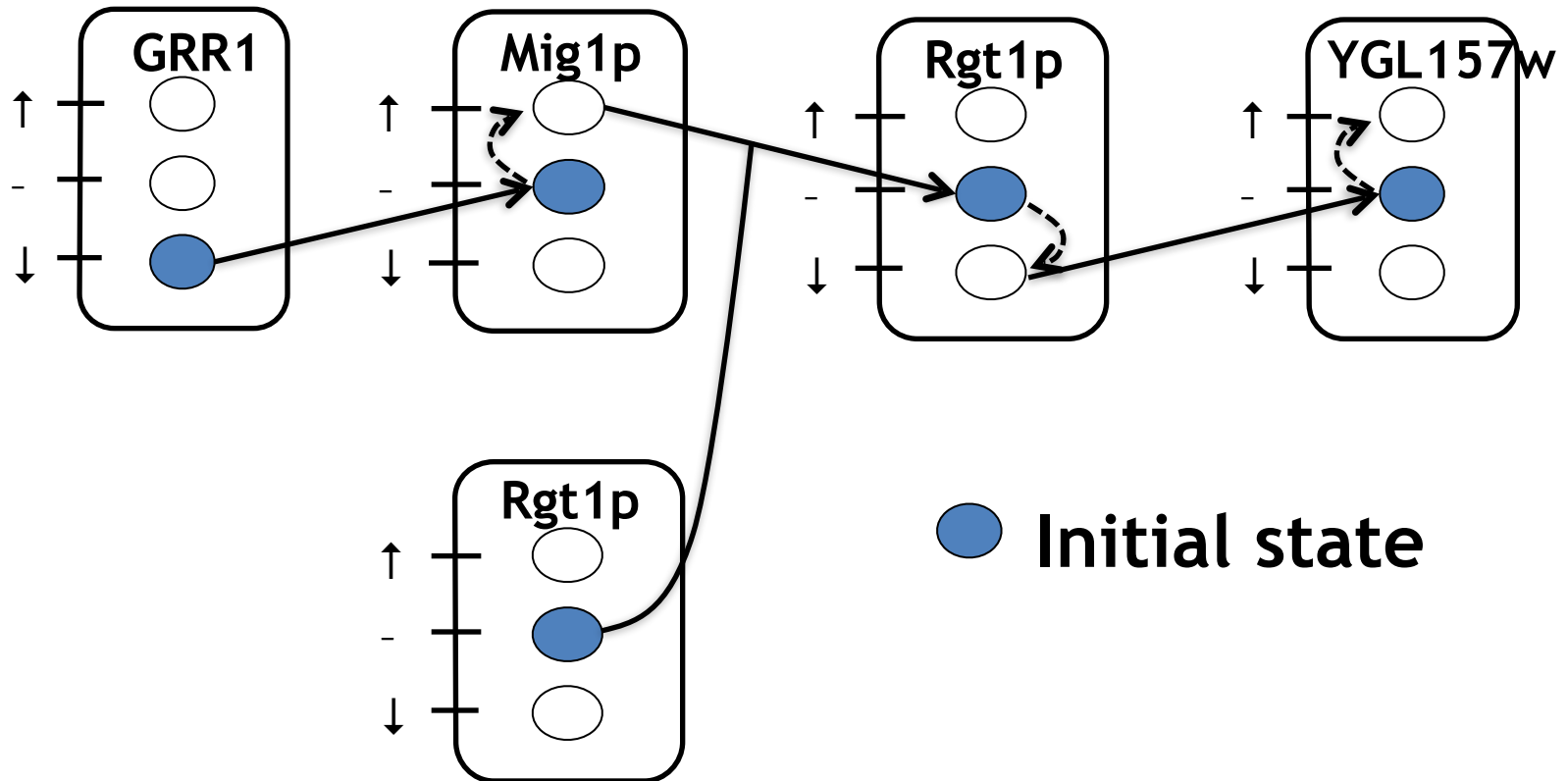
- **Asynchronous versus synchronous semantics, w.r.t. the addition of priorities**
- **Compare 4-valued logics with existing approaches with ODEs**
- **Interest for a cut-sets based approach**

# Cut-sets in Process Hitting

- **Sets of necessary processes** that, should they be disabled, would prevent the considered reachability
- Useful to **refute a model**: if a cut set computed from the model does not prevent the reachability in the concrete (modeled) system, then it is a proof that there exists concrete behaviors that are not reproducible by the model.
- See (Paulevé et al., 2014) and Loïc's talk last year

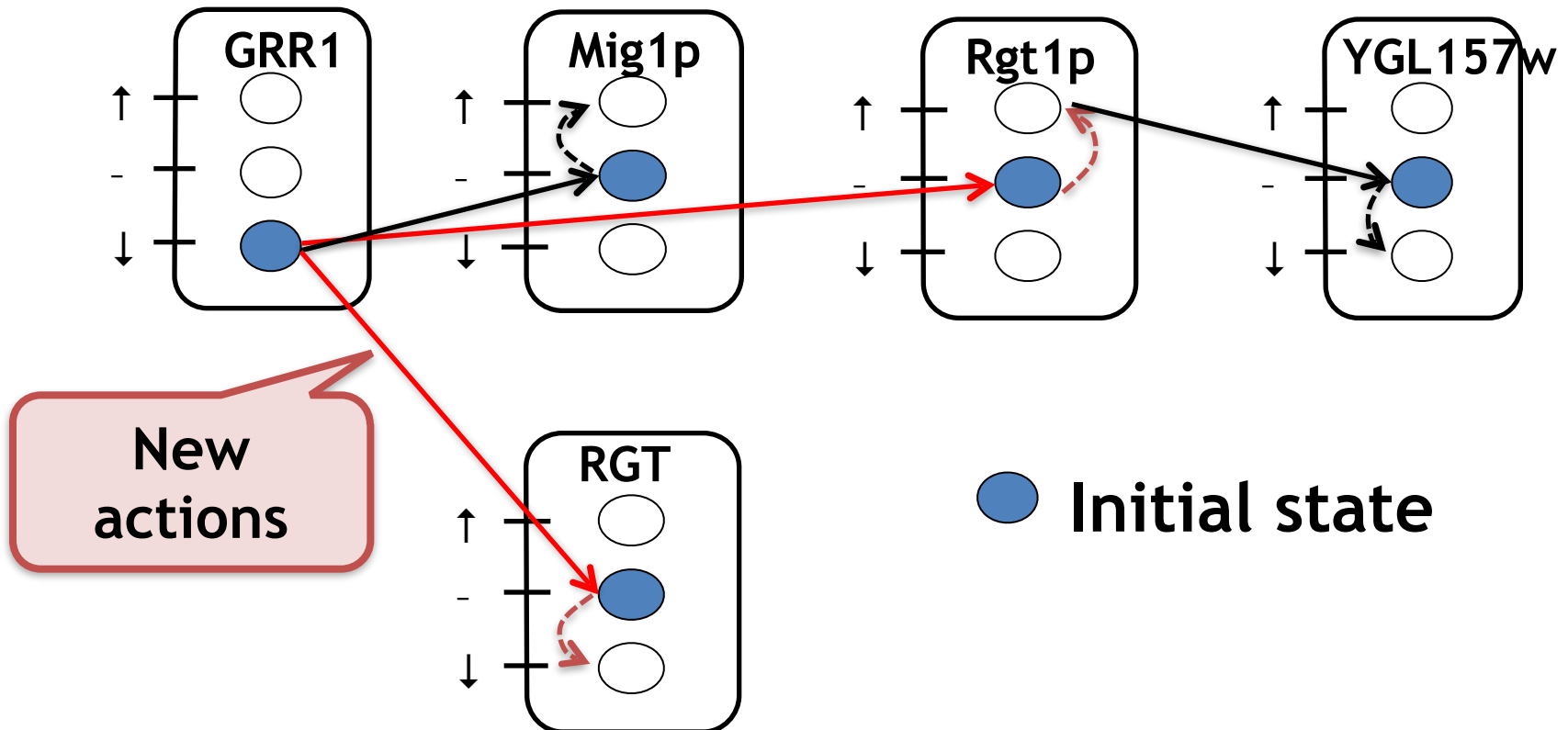
# Problem setting (for abduction in process hitting)

- Finding actions for explaining the observation with the background theory (Boolean network)



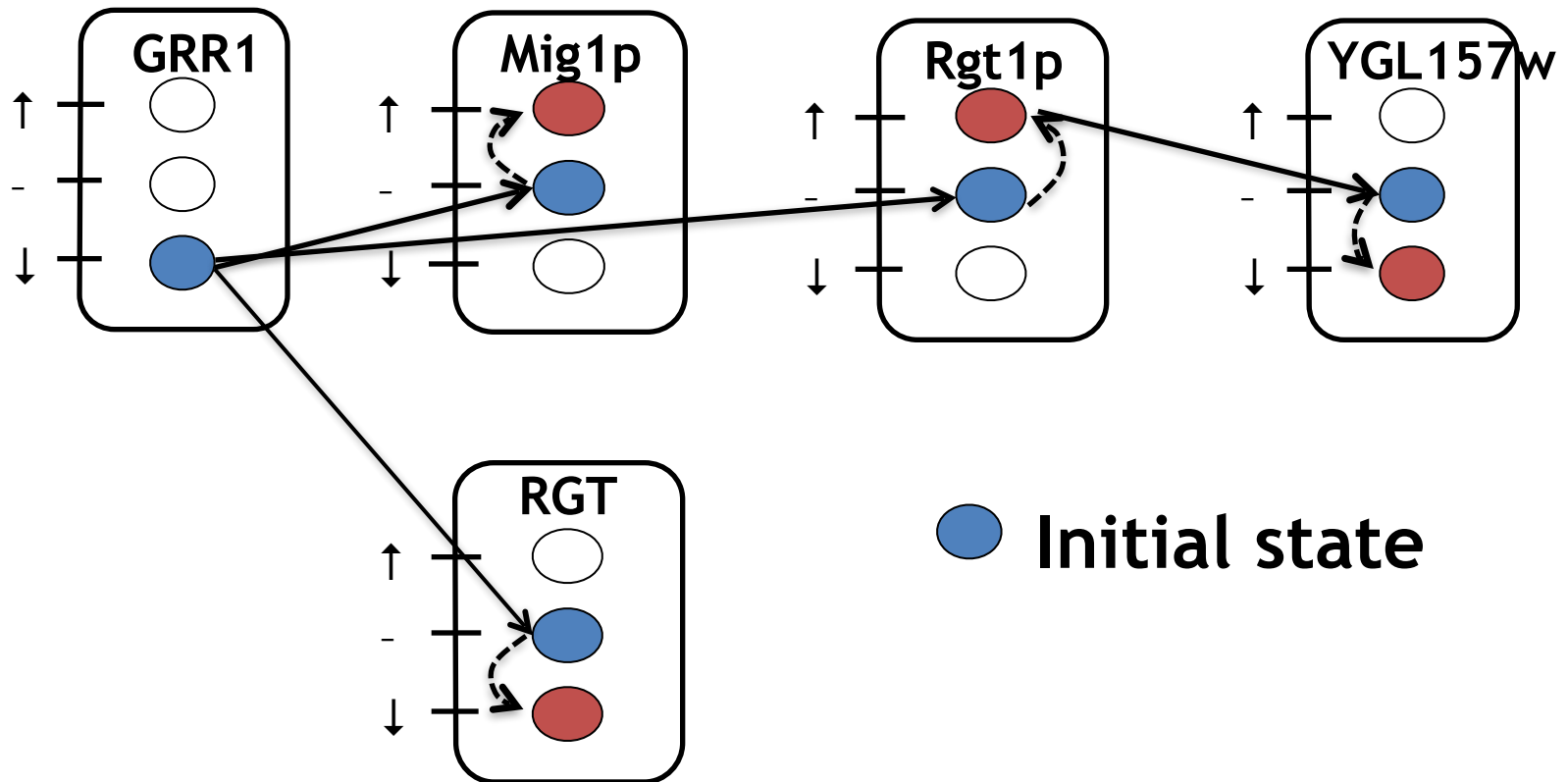
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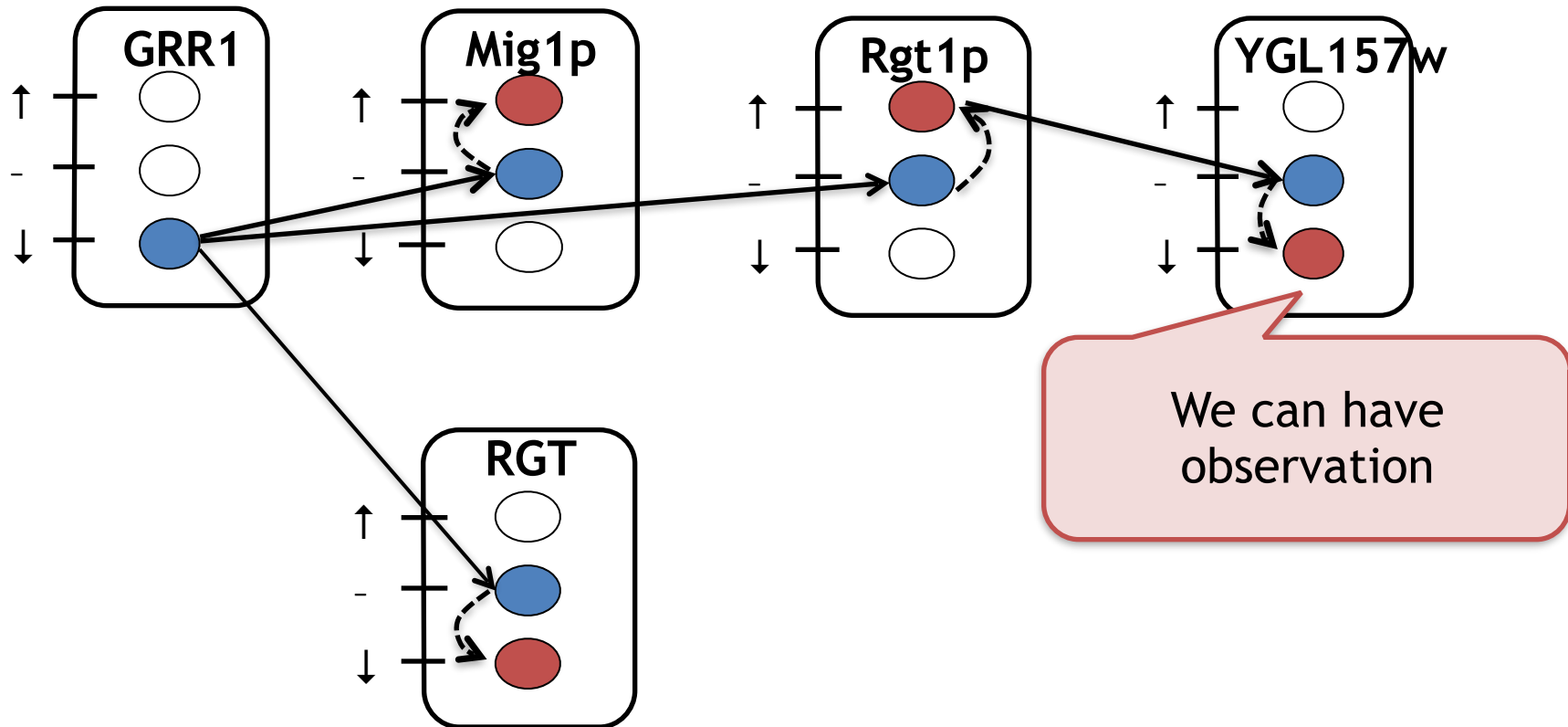
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# Research plan and future work

- **Formalize** an algorithmic approach to tackle this completion problem
- Study models with **feedback loops** and extend the principle of 4-valued logics
- Tackle models with **time series data** as input